Meanings for Multiplication

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There are 4 rows of 5.

Addition sentence:

5 + 5 + 5 + 5 = 20

Multiplication sentence:

$$4 \times 5 = 20$$

There are 3 boxes. There are 7 books in each box.







There are 3 groups of 7.

Addition sentence:

$$7 + 7 + 7 = 21$$

Multiplication sentence:

$$3 \times 7 = 21$$

Write an addition sentence and a multiplication sentence for each picture.





Write a multiplication sentence for each addition sentence.

3. 10 + 10 + 10 + 10 = 40

4	3	+	3	+	3	+	3	+	3	+	3	=	18
-	\sim		0		0		0		0	- 1	0		10

5. Number Sense Explain how multiplication can help you find 7 + 7 + 7.

Patterns in Multiplying by 0, 1, 2, 5, and 9

Pattern Example All multiples of two are even numbers. 2, 18, 44 All multiples of 5 end in 0 or 5. 25, 100, 220 For all multiples of nine, the sum of 27 2 + 7 = 9the digits is always a multiple of 9. 63 6 + 3 = 9The product of any number and zero $17 \times 0 = 0$ is zero. The product of any number and one $32 \times 1 = 32$ is that number. Two numbers can be multiplied in any $4 \times 5 = 20^{\circ}$ order and the product will be the same. $5 \times 4 = 20$

- 1. 9 × 5
- 2. 2 × 8
- 3. 8 × 5
- **4.** 9 × 0

- **5.** 9 × 3
- 6. 7 · × 2
- 7. 0 × 3
- 8. 1 × 56

9. How many baseball cards are in 4 packages?

Item	Number in Package			
Baseball cards	5			
Stickers	2			
Coupon	1			

- 10. How many stickers do you get if you buy 9 packages?
- **11.** How many coupons do you get if you buy 7 packages?

Using Known Facts to Find Unknown Facts

You can use breaking apart to find a product.

Find 4×5 .

4 groups of 5 are the same as 2 groups of 5 and 2 groups of 5.

$$4 \times 5 = 2 \times 5 + 2 \times 5$$

= 10 + 10
= 20

Use breaking apart to find each product.

Compare. Use <, >, or = to fill in each \bigcirc .

9.
$$7 \times 6 \bigcirc 5 \times 7$$

10.
$$9 \times 4 \bigcirc 4 \times 9$$

11.
$$4 \times 4$$
 2×8

12.
$$7 \times 8 \bigcirc 9 \times 5$$

Here are some easy ways to multiply numbers by 10, 11, and 12.

Multiples of 10

Any whole number multiplied by 10 will always equal that number with an additional zero in the ones place.

For example,
$$2 \times 10 = 20$$
, $22 \times 10 = 220$, and $220 \times 10 = 2,200$.

You can also break apart equations to help find products.

Multiples of 11

To find 12×11 , think of 11 as 10 + 1.

$$12 \times 10 = 120$$
, $12 \times 1 = 12$, $120 + 12 = 132$, so $12 \times 11 = 132$.

Multiples of 12

To find 6×12 , think of 12 as 10 + 2.

$$6 \times 10 = 60$$
, $6 \times 2 = 12$, $60 + 12 = 72$, so $6 \times 12 = 72$.

1.
$$5 \times 11 =$$
 _____ **2.** $12 \times 4 =$ ____ **3.** $10 \times 9 =$ ____

4.
$$7 \times 12 =$$
 _____ **5.** $12 \times 11 =$ ____ **6.** $8 \times 10 =$ ____

7. Number Sense Explain how 9×10 can help you find 9×11 .

There are 11 players on the field for each football team during a game. How many players would there be on

- 8. 4 teams?
- 9. 8 teams?
- 10. 10 teams?
- 11. 11 teams?

PROBLEM-SOLVING STRATEGY

Make a Table

Complete the table to solve the problem. Write the answer in a complete sentence.

1. The grocery store is having a sale on canned vegetables. If you buy 1 can, you get 2 free. How many cans do you need to buy to get 16 cans free?

Cans purchased	1	2	3	4	5	6	7	8	9
Free cans	2	4							

2. Grandma wanted to help Jennifer learn to multiply. On the first day of Jennifer's visit, Grandma gave her 2 charms for her charm bracelet. On the second day, Grandma gave Jennifer 4 charms. On the third day, she gave Jennifer 8 charms. How many charms did Grandma give Jennifer on the sixth day of her visit?

Day	1	2	3	4	5	6	7
Charms	2	4	8				

For Exercise 3, make a table. Use it to find the answer.

3. Juan decided to raise money for his camping trip by selling lemonade. He charged \$1.00 for 1 glass, \$1.25 for 2 glasses, \$1.50 for 3 glasses, and so on. How much money did Juan charge for 5 glasses of lemonade?

Meanings for Division

Draw pictures to solve each problem.

1. There are 12 small gift bags. Each bag can hold 1 toy and some stickers. There are 36 stickers. If an equal number of stickers is put in each bag, how many stickers will be in each bag?

2. One egg carton holds 12 eggs. How many cartons are you able to fill with 60 eggs?

3. There are 21 students in Mr. Tentler's class. The students divided themselves evenly into 3 groups.

How many students are in each group?

Test Prep

- **4.** Calvin read an 18-page chapter in his social studies book in 2 hours. If he read the same number of pages each hour, how many pages did he read per hour?
 - A. 3 pages
- B. 6 pages
- C. 9 pages
- D. 12 pages
- 5. Writing in Math The class is planning a party. The pizza restaurant cuts each pizza into 8 slices. There are 32 students. How many pizzas does the class need to order for each student to have a slice? Explain.

Relating Multiplication and Division

Multiplication and division are related, just like addition and subtraction are related.

This is the fact family for 5, 6, and 30:

$$5 \times 6 = 30$$

$$30 \div 6 = 5$$

$$6 \times 5 = 30$$

$$30 \div 5 = 6$$

Complete each fact family.

Write a fact family for each set of numbers.

- **5.** 7, 4, 28 _____
- **6.** 5, 8, 40 _____
- 7. Number Sense What multiplication facts are part of the fact family for $12 \div 3 = 4$?

Division Facts

Thinking about multiplication facts can help when you want to divide. For example: Sunny and her father are packing oranges. They have 42 oranges. Each crate holds 6 oranges. How many crates do they need?

What You Think	What You Say	What You Write
What number times 6 = 42?	42 divided by 6 is what number?	42 ÷ 6 = 7
× 6 = 42	or	or
7 times 6 equals 42 7 × 6 = 42	How many times does 6 go into 42?	6)42

9. Reasoning If $66 \div 6 = 11$, what is $66 \div 11$? Explain.

10. A ticket to ride the roller coaster costs \$3. How many rides can you get for \$15?

11. Steve spends \$24 on books. Books cost \$8 each. How many books did Steve buy?

R 3-9

Special Quotients

There are special rules for dividing numbers by 1 and by 0.

Rule: A number divided by 1 is that number.

Examples:
$$4 \div 1 = 4$$

$$55 \div 1 = 55$$

Rule: A number divided by itself (except 0) is 1.

Examples:
$$17 \div 17 = 1$$

$$135 \div 135 = 1$$

Rule: Zero divided by a number (except 0) is 0.

Examples:
$$0 \div 4 = 0$$

$$0 \div 15 = 0$$

Rule: You cannot divide a number by zero.

Examples:
$$7 \div 0$$
 cannot be done.

Compare. Use >, <, or = for each \bigcirc .

9.
$$6 \div 6$$
 3 ÷ 3

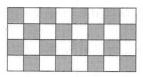
13.
$$5 \div 5$$
 0 ÷ 5

19. Number Sense If $a \div b = 0$, what do you know about a?

Tile Floor Darren is laying a tile floor in the hallway. The pattern for the floor is shown to the right.

First, use Darren's tile floor to write a multiplication story for $4 \times 8 = 32$.

Second, use Darren's tile floor to write a division story for $32 \div 4 = 8$.



Darren's tile floor has 4 rows with 8 pieces of tile in each row. How many pieces of tile are there in all?

Darren has 32 small triangles. He needs 4 for each shaded square. How many shaded squares can he make with the small triangles?

Use the data in the table to write a multiplication or a division story for each number fact. Solve.

Building Supplies	Number in a Box		
Fasteners	6		
Bolts	12		

1. 6 × 4

2. 12 ÷ 4

PROBLEM-SOLVING SKILL

Multiple-Step Problems

Lawn Cutting Chad and his brother Brad cut lawns in their neighborhood to make money. They charge \$20 per lawn. One weekend, Brad cut 4 lawns, and Chad cut 3 lawns. How much money did they earn altogether?

Solution One

Hidden Question: How many lawns did they mow altogether?

Chad cut 3 lawns, Brad cut 4 lawns.

$$3 + 4 = 7$$

They cut 7 lawns.

Question in the Problem: How much money did they earn altogether?

7 lawns \times \$20 = \$140

Chad and Brad earned \$140.

Solution Two

Hidden Question 1: How much money did Chad get for cutting lawns?

$$3 \times $20 = $60$$

Hidden Question 2: How much money did Brad get for cutting lawns?

$$4 \times \$20 = \$80$$

Question in the Problem: How much money did they earn altogether?

$$$60 + $80 = $140$$

Chad and Brad earned \$140.

Write and answer the hidden question or questions. Then solve the problem. Write your answer in a complete sentence.

 Keisha sold 8 ribbons. Then she sold 6 pins. The ribbons sold for \$3; the pins sold for \$2. How much money did Keisha make?

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How to evaluate a multiplication expression:

Evaluate 5n for n = 8. Remember, 5n means the same as $5 \times n$.

First, substitute 8 for n. Then multiply.

$$5 \times n = ?$$

$$5 \times 8 = ?$$

$$5 \times 8 = 40$$

How to evaluate a division expression:

Evaluate
$$g \div 6$$
 for $g = 42$.

First, substitute 42 for g. Then divide.

$$g \div 6 = ?$$

$$42 \div 6 = ?$$

$$42 \div 6 = 7$$

How to evaluate expressions with more than one operation:

Evaluate
$$(4f) + 7$$
 for $f = 5$.

First, substitute 5 for f. Then do the computations inside the parentheses first.

$$(4 \times f) + 7 = ?$$

$$(4 \times 5) + 7 = ?$$

$$20 + 7 = 27$$

Evaluate each expression for m = 4.

2.
$$\frac{m}{2} =$$

3.
$$20 \div m =$$

4.
$$(7m) + 2 =$$

5. Number Sense Write an expression that equals 50 for
$$n = 10$$
.

Evaluate each expression for w = 7.

6.
$$5 \times w =$$

7.
$$7 \div w =$$

8.
$$9w =$$

9.
$$3 \times (2 + w) =$$

Evaluate each expression.

10.
$$8 \times (4 + k)$$
 for $k = 2$

11.
$$h \div (6 \times 1)$$
 for $h = 30$

Find a Rule

Complete the table. Start with the number in the IN column. What rule tells you how to find the number in the OUT column? Write the rule.

IN	TUO
2	10
4	20
6	30
8	
n	

What You Think

$$2 \times 5 = 10$$

 $4 \times 5 = 20$
 $6 \times 5 = 30$
 $8 \times 5 = 40$

A rule is multiply by 5.

What You Write

IN	OUT	
2	10	
4	20	
6	30	
8	40	
n	n×5	

The rule multiply by 5 is written as $n \times 5$.

Complete each table. Write the rule.

1.	In	20	25	35	55	n
	Out	4	5	7		2540

2.	In	.3	5	7	9	n
	Out	9	15	21		

3.	In	2	5	7	10	n
	Out	14	35	49		

Solving Multiplication and Division Equations

To solve an equation that has a variable you need to test several numbers for the variable. Find the one number that makes the equation true.

Solve the equation 4n = 28 by testing these values for n: 5, 6, and 7.

Try	n = 5	n = 6	n = 7
Find 4n	$4 \times 5 = 20$	$4 \times 6 = 24$	$4 \times 7 = 28$
Does 4n = 28?	No	No	Yes

The solution to the equation is n = 7, because $4 \times 7 = 28$.

Solve the equation $g \div 5 = 9$ by testing these values for g: 30, 45, and 60.

Try	g = 30	g = 45	g = 60	
Find $g \div 5$	$30 \div 5 = 6$	$45 \div 5 = 9$	60 ÷ 5 = 12	
Does $g \div 5 = 9$?	No	Yes	No	

The solution to the equation is g = 45, because $45 \div 5 = 9$.

Solve each equation by testing these values for k: 2, 4, and 6.

1.
$$k \div 2 = 3$$

3.
$$36 \div k = 9$$

Solve each equation by testing these values for n: 12, 16, and 24.

5.
$$n \div 6 = 4$$

6.
$$n \div 4 = 4$$

7.
$$n \times 2 = 24$$

8.
$$n \div 4 = 3$$

9. Number Sense What is the value of b in the equation $b \times 7 = 63$? How do you know?

PROBLEM-SOLVING APPLICATIONS

The Party

Alberto is planning a party. He needs to purchase the following items:

How much will Alberto have to spend if he purchases 2 paper tablecloths?

$$2 \times \$11 = \$22$$

He will have to spend \$22.

Party Supplies

Item	Price	
Napkins	\$2	
Paper plates	\$5	
Cups	\$9	
Balloons	\$10	
Paper tablecloth	\$11	
Juice	\$12	

Use the chart above to answer the following questions.

- **1.** Alberto purchased 6 packages of paper plates. The addition sentence that shows how much he spent is 5+5+5+5+5+5=30. Write the multiplication sentence for this addition sentence.
- Since many people are coming to the party, Alberto purchased 9 packages of napkins. Complete the fact family.

How much did Alberto spend on

- 3. 5 bottles of juice?
- 4. 7 packages of cups?
- 5. 4 packages of paper plates?
- **6.** Alberto spent \$50 on balloons. How many bags of balloons did he purchase?