

Unit 8 Objective 2 Remediation

Solve Proportions Using Cross Multiplication

Using Cross Products in Proportions

An equation in which two ratios, $\frac{a}{b}$ and $\frac{c}{d}$, are equal is called a proportion.

In the proportion $\frac{a}{b} = \frac{c}{d}$, where $b \neq 0$ and $d \neq 0$, b and c are the means, and a and d are the extremes. The cross products of the proportion $\frac{a}{b} = \frac{c}{d}$ are ad and bc .

In any true proportion, cross products are equal. That is, $ad = bc$.

Solving Proportions

You can use cross products to write and solve equations.

➤ **Example 1**

$$\text{Solve } \frac{10}{12} = \frac{25}{x}$$

Solution

The cross products are $10x$ and $12 \cdot 25$, or 300 .

$10x = 300$ Set the cross products equal to one another.

$$\frac{10x}{10} = \frac{300}{10}$$

$$x = 30$$

➤ **Example 2**

$$\text{Solve } \frac{x}{1.5} = \frac{-3}{2}$$

Solution

The cross products are $2x$ and $-3 \cdot 1.5$, or -4.5 .

$2x = -4.5$ Set the cross products equal to one another.

$$\frac{2x}{2} = \frac{-4.5}{2}$$

$$x = -2.25$$

➤ **Example 3**

$$\text{Solve } \frac{5}{2} = \frac{x+1}{4}$$

Solution

The cross products are $2(x+1)$, or $2x + 2$ and $5 \cdot 4$, or 20 .

$2x + 2 = 20$ Set the cross products equal to one another.

$$2x + 2 - 2 = 20 - 2$$

$$\frac{2x}{2} = \frac{18}{2}$$

$$x = 9$$

Try Some! Solve for the variable.

1.) $\frac{6}{7} = \frac{5.4}{b}$

6.) $\frac{8}{1.6} = \frac{e}{2}$

2.) $\frac{a}{5} = \frac{2}{10}$

7.) $\frac{6}{7} = \frac{5.4}{b}$

3.) $\frac{18}{p} = \frac{-9}{25}$

8.) $\frac{x+2}{7} = \frac{4}{2}$

4.) $\frac{5}{6} = \frac{20}{r}$

9.) $\frac{180}{-9} = \frac{60}{n}$

5.) $\frac{1.5}{8} = \frac{k}{32}$

10.) $\frac{4}{7} = \frac{4}{x+2}$