## Keystone Review Module I

The Keystone Exam is broken into 2 Modules.
Module $1 \quad$ Module 2

- Operations with Real Numbers and Expressions
- Functions
- Linear Equations
- Coordinate Geometry
- Linear Inequalities
- Data Analysis


## Operations with Real Numbers and Expressions

Under this topic you will be asked to...

- Compare/Order Real Numbers
- Simplify Square Roots
- Find GCF and LCM
- Simplify Expressions Using Exponent Properties
- Simplifying Algebraic Expressions
- Factoring


## Linear Equations

Under this topic you will be asked to...

- Write a Linear Equation with One Variable
- Use the Properties of Equality to Solve Linear Equations with One Variable
- Write a Linear Equation with Two Variables
- Write a System of Linear Equations with Two Variables
- Solve a System of Linear Equations with Two Variables


## Linear Inequalities

Under this topic you will be asked to...

- Solve a Linear Inequality
- Solve a Compound Inequality
- Solve a System of Linear Inequalities


## Writing a Linear Equation with One Variable

Sometimes a linear equation is described in words. You must be able to translate the words into a mathematical equation. In most problems, a consistent amount that does not change will represent the $y$-intercept. An amount that will change in relation to another quantity represents the slope. We use slopeintercept form $\boldsymbol{y}=\boldsymbol{m} \boldsymbol{x}+\boldsymbol{b}$ to write the equation.

| Words that indicate the Slope | Words that indicate the $\boldsymbol{y}$-intercept |
| :---: | :---: |
| per | initial amount |
| each | daily fee |
| every |  |
| monthly | starting amount |
| rate | set-up fee |

Felix buys a carpet for $\mathbf{\$ 2 3 0}$. The price is $\mathbf{\$ 3 . 5 0}$ per square foot. If Felix had a special discount coupon for $\$ 50$ off, which linear equation could be used to find the area, $A$, of the carpet?
A. $230=3.5 A+50$
B. $50=3.5 A-230$
C. $230=3.5 A-50$
D. $50=230-3.5 A$

Answer:

An online booking agency charges for tickets and includes a ticketing fee for each order. The total charge, $c$, in dollars, for any number of tickets, $t$, is described by the function $c=20 t+4$. Which statement is true?
A. The cost of 20 tickets is $\$ 80$.
B. The cost of 4 tickets is $\$ 20$.
C. Each ticket costs $\$ 20$ and the ticketing fee is $\$ 4$.
D. Each ticket costs $\$ 4$ and the ticketing fee is \$20.

Answer:

## Using Properties of Equality to Solve Linear Equations with One Variable

When solving linear equations, we use the properties of equality.

- Addition Property of Equality
- Subtraction Property of Equality
- Multiplication Property of Equality
- Division Property of Equality

Often we may need to simplify an equation before we solve. You may need to...

- Remove parentheses using the distributive property
- Collect like terms
- Isolate the variable on one side of the equation

The steps Derek used to solve an equation are shown below:
Solve:

$$
0.4 x+5+0.2 x=17
$$

Step 1:
$0.4 x+0.2 x+5=17$
Step 2:
0. $6 x+5=17$

Step 3:
$0.6 x=12$
Step 4: $\quad x=20$
Which properties justify Step 1 and Step 3?
A. Step 1: Distributive Property
Step 3: Division Property of Equality
B. Step 1: Distributive Property
Step 3: Subtraction Property of Equality
C. Step 1: Commutative Property of Addition
Step 3: Division Property of Equality
D. Step 1: Commutative Property of Addition
Step 3: Subtraction Property of Equality

Answer:

What is the solution to the linear equation $\frac{3}{4} x-5=10$ ?
A. $y=\frac{15}{4}$
B. $y=\frac{20}{3}$
C. $y=\frac{45}{4}$
D. $y=20$

Answer:

## Solving a Linear Inequality

Solving a linear inequality is the same as solving a linear equation except you REVERSE the inequality sign if you are multiplying or dividing by a negative number. The solution set is represented by a graph.

| $x>0$ <br> $x$ is greater than zero | $x<0$ <br> $x$ is less than zero | $x \geq 0$ <br> $x$ is greater than or equal to zero | $x \leq 0$ <br> $x$ is less than or equal to zero |
| :---: | :---: | :---: | :---: |
| $\stackrel{-3}{3}$ | $\stackrel{-3}{\stackrel{3}{*}}$ | $\stackrel{-3}{\overleftrightarrow{3}}$ | $\stackrel{-3}{\overleftrightarrow{3}}$ |

What is the solution to the inequality $-\frac{y}{5}+6>2$ ?
A. $y<-20$
B. $y<20$
C. $y>-20$
D. $y>20$

## Answer:

Which graph shows the solution set to the inequality $3(3-x)<-12$ ?
A.

C.


## Answer:

Recall the phrases that represent the different inequality symbols.

|  | $\geq$ | $\leq$ |  |
| :--- | :--- | :--- | :--- |
| is more than <br> is greater than <br> is larger than <br> above | minimum <br> at least <br> is not less than <br> no less than <br> not smaller than | is smaller than <br> is less than <br> is fewer than <br> below | maximum <br> at most <br> is not more than <br> no more than <br> is not greater than |

Write the inequality that models the situation. Solve and then interpret your solution.
Ore Valley Elementary school is having a fall carnival. Admission into the carnival is $\$ 3$ and each game inside the carnival costs $\$ 0.25$. Tanner has no more than $\$ 10$ to spend. What is the maximum number of games he can play?

Answer:

Rebecca wants to order some DVDs from Amazon. The DVDs cost $\$ 7.98$ each and there is a shipping charge of $\$ 5$. She can spend no more than $\$ 100$. What is the maximum number of DVDs she can buy?

Answer:

## Solving a Compound Inequality

A compound inequality is formed when two inequalities are joined by the words "and" or "or".

| Conjunction | Disjunction |
| :--- | :--- |
|  |  |
| The solution must satisfy both inequalities for the <br> conjunction to be true. <br> Look for the overlap or intersection in the graph <br> of the two inequalities to be our solution. | The solution must satisfy either of the inequalities <br> for the disjunction to be true. |
| The two inequalities together on the same graph |  |
| or the union of the graphs will be our solution. |  |

Which graph shows the solution to $7<-3-2 x<11$ ?
A.

C.


Answer:
B.

D.


What is the solution to the compound inequality $5+3 x<2$ or $2 x-7>-3$ ?
A. $x<-1$ or $x>2$
B. $-1<x<2$
C. $x<-1$ or $x>-5$
D. $-1<x<-5$

## Answer:

## Writing a Linear Equation with Two Variables

Jackson has $75 \$$ in dimes, $d$, and nickels, $n$, in his pocket. Which equation could be solved to find the possible combinations of dimes and nickels Jackson has?
A. $75=d+n$
B. $75=d n$
C. $75=10 d \cdot 5 n$
D. $75=10 d+5 n$

## Answer:

The growth of a kitten is described by the equation $y=2.5 x+4$, where $y$ represents the kitten's weight in ounces $x$ weeks after it was born. What is the meaning of the fact that the point $(4,14)$ lies on the graph of the equation?
A. The kitten had an initial weight of 4 ounces.
B. The kitten is growing at a rate of 4 ounces per week.
C. The kitten weighed 4 ounces when it was 14 weeks old.
D. The kitten weighed 14 ounces when it was 4 weeks old.

Answer:

## Writing a System of Linear Equations with Two Variables

Georgia needs to print posters for a community event. Stellar Printers will charge Georgia a $\$ 300$ set-up fee plus $\mathbf{\$ 1}$ per poster. Artemis Printers will charge Georgia a $\mathbf{\$ 2 0 0}$ set-up fee plus $\mathbf{\$ 1 . 5 0}$ per poster. Write a system of linear equations where $y$ is the cost in dollars and $x$ is the number of posters.
A. $\left\{\begin{array}{c}y=300 x \\ y=200 x+1.5\end{array}\right.$
B. $\left\{\begin{array}{c}y=x+300 \\ y=1.5 x+200\end{array}\right.$
C. $\left\{\begin{array}{c}y=x-300 \\ y=1.5 x-200\end{array}\right.$
D. $\left\{\begin{array}{c}x=y+300 \\ x=1.5 y+200\end{array}\right.$

Answer:

Stephen bought a total of 8 pounds of peanuts and cashews. Peanuts, $p$, cost $\$ 2$ per pound and cashews, $c$, cost $\$ 5$ per pound. The total amount Stephen spent on the peanuts and cashews was $\$ 25$. Which system of equations could be solved to find how many pounds of peanuts Stephen bought?
A. $\left\{\begin{array}{c}2 p+5 c=25 \\ p+c=8\end{array}\right.$
B. $\left\{\begin{array}{c}5 p+2 c=25 \\ p+c=8\end{array}\right.$
C. $\left\{\begin{array}{c}2 p+5 c=8 \\ p+c=25\end{array}\right.$
D. $\left\{\begin{array}{c}2 p=8 \\ 5 c=25\end{array}\right.$

Answer:

## Solving a System of Linear Equations with Two Variables

A System of Linear Equations is two or more linear equations with multiple variables.
The solution of a system of linear equations is the point where the two lines intersect.
We learned three ways to solve a system of linear equations.

1. Graphing
2. Substitution
3. Elimination

## Solving by Graphing

When in the system of linear equations is graphed, the solution is the point of intersection of the two lines.

What is the solution of the system of equations graphed below?

A. $(0,-1)$
B. $(0,1)$
C. $(2,3)$
D. $(3,2)$

## Answer:

## Solving by Substitution

1. Solve one of the equations for one of its variables.
2. Substitute the expression from step 1 into the OTHER equation and solve for the other variable.
3. Substitute the value from step 2 into the one of the original equations and find the value of the second variable.

What is the solution to the system of equations shown below?

$$
\left\{\begin{array}{c}
2 x+y=9 \\
x=3-y
\end{array}\right.
$$

A. $(1,7)$
B. $(4,1)$
C. $(2,5)$
D. $(6,-3)$

Answer:

1. Multiply one or both of the equations by a number so that the coefficients of one of the variables are opposites
2. Add the equations from step 1 together. Combining the equations will eliminate one of the variables.
3. Solve for the remaining variable.
4. Substitute the value from step 3 into the one of the original equations and find the value of the second variable.

What is the solution to the system of equations shown below?

$$
\left\{\begin{array}{c}
4 x-y=7 \\
-4 x-2 y=2
\end{array}\right.
$$

A. $(-1,3)$
B. $(1,-3)$
C. $(2,-3)$
D. $(3,5)$

## Answer:

## Solving a System of Linear Inequalities

A system of linear inequalities is graphed on the same coordinate plane. The solutions of this problem are the points located in the overlap of the shaded region.


Graph the solution of the system of linear inequalities $\left\{\begin{array}{c}x+2 y>-6 \\ x \geq-2\end{array}\right.$


State whether or not the given points are solutions of the system of linear inequalities below.

1. $(0,0)$
2. $(-1,2)$
3. $(0,-3)$

4. $(2,0)$
5. $(3,3)$

Which graph represents the solution of the system of inequalities shown below?

$$
\left\{\begin{array}{c}
y \geq 2 x-3 \\
x+y<4
\end{array}\right.
$$

A.

B.

C.

D.


In Lewis Carroll's "Through the Looking Glass" Tweedledum says, "The sum of your weight and twice mine is 361 pounds." Tweedledee replies, "The sum of your weight and twice mine is 362 pounds." Write a system of linear equations and find both of their weights.

Let $x=$ Tweedledee's weight
Let $y=$ Tweedledum's weight

Answer:

Lucy tells her little brother Jack that she is holding $\mathbf{2 0}$ coins consisting of dimes and quarters. They have a total value of $\mathbf{\$ 4 . 1 0}$. She tells Jack that she will give him the coins if he can tell her how many of each she is holding. Solve this problem for Jack.

Let $d=$ number of dimes
Let $q=$ number of quarters
Answer:

A clothing manufacturer has 900 yards of cotton to make shirts and pajamas. A shirt requires 1 yard of fabric and a pair of pajamas requires $\mathbf{2}$ yards of fabric. It takes $\mathbf{2}$ hours to make a shirt and $\mathbf{3}$ hours to make the pajamas, and there are $\mathbf{1 2 0 0}$ hours available to make the clothing.
a. Write a system of linear inequalities where $x$ is the number of shirts and $y$ is the number of pajamas.
b. Graph the solution. Be sure to label your axes.

c. How many shirts and pajamas can be manufactured? Give three solutions.

Zach's high school theater can seat at most 400 people. Adult tickets are $\mathbf{\$ 5}$ and student tickets are \$2. How many adult tickets and student tickets must be sold so that the school makes at least $\$ 1,000$ ? Let $x=$ number of adult tickets sold and $y=$ number of student tickets sold.
a. Write a system of inequalities to represent the problem.
b. Graph the solution. Be sure to label your axes.

c. Give three possible combinations of adult and student tickets that could be sold so the school meets its goal.

